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Turbulence Detection in the Atmospheric Boundary Layer Using Coherent Doppler Wind Lidar and Microwave Radiometer

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Abstract: The refractive index structure constant (C_n^2) is a key parameter used in describing the influence of turbulence on laser transmissions in the atmosphere. Three different methods for estimating C_n^2 were analyzed in detail. A new method that uses a combination of these methods for continuous C_n^2 profiling with both high temporal and spatial resolution is proposed and demonstrated. Under the assumption of the Kolmogorov "2/3 law", the C_n^2 profile can be calculated by using the wind field and turbulent kinetic energy dissipation rate (TKEDR) measured by coherent Doppler wind lidar (CDWL) and other meteorological parameters derived from a microwave radiometer (MWR). In a horizontal experiment, a comparison between the results from our new method and measurements made by a large aperture scintillometer (LAS) is conducted. The correlation coefficient, mean error, and standard deviation between them in a six-day observation are 0.8073, 8.18 × 10⁻¹⁶ m^{-2/3} and 1.27 × 10⁻¹⁵ m^{-2/3}, respectively. In the vertical direction, the continuous profiling results of C_n^2 and other turbulence parameters with high resolution in the atmospheric boundary layer (ABL) are retrieved. In addition, the limitation and uncertainty of this method under different circumstances were analyzed, which shows that the relative error of C_n^2 estimation normally does not exceed 30% under the convective boundary layer (CBL).

Keywords: atmospheric turbulence; coherent Doppler wind lidar; microwave radiometer; turbulent kinetic energy dissipation rate; buoyancy term; Richardson number; integral scale; C_n^2 profile



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1. Introduction

Turbulence analysis is meaningful in many fields, such as astronomy [1], aviation safety [2], optical communication technology [3], laser weapon [4], wind field retrieval [5], air pollution [6], oceanography [7], etc. In astronomy, due to the existence of atmospheric turbulence, the star images seen in astronomical observations often jitter and flicker, and increasing the aperture of the telescope in ground-based observations cannot achieve the expected results. To reduce the effects, researchers need to seek sites with high altitudes or locations such Dome A in Antarctica [1], where the atmospheric boundary layer (ABL) is thin. In addition, in areas of Free-Space Optical (FSO) communications and laser ranging, the fluctuation of the refractive index caused by atmospheric turbulence will affect the coherence of the laser beam through the optical angle-of-arrival fluctuation, laser beam wander and scintillation [8], etc. These phenomena will bring uncertain variances and reduce the detection efficiency of these systems.

There are several parameters normally used to describe the turbulence from the aspect of dynamics or thermodynamics, for example, the Reynolds number, turbulence kinetic Remote Sens. 2022, 14, 2951 2 of 25

energy, Richardson number, integral scale, temperature structure constant, refractive index structure constant, etc. Among all these parameters, the refractive index structure constant C_n^2 is the one that contains both dynamics and thermodynamics information and most directly represents the fluctuation intensity of the spatial refractive index, which makes it unique and vital, especially in optical turbulence research. At present, there are some common methods for C_n^2 detection.

For instance, in areas of astronomy and satellite-ground laser communication, C_n^2 profiles can be obtained by Slope Detection and Ranging (SLODAR) [9], Coupled Slope and Scintillation Detection and Ranging (CO-SLIDAR) [10], etc. [11–13]. The empirical models that represent the average characteristics of different regions are normally used for comparison, such as the Hufnagel-Valley (HV) profile model [14–17].

In addition, using the Radiosonde and sounding balloon, turbulence profile can be acquired at high spatial resolutions [18–22]. In the near-surface, researchers mostly use the relationship between C_n^2 and the temperature structure constant C_T^2 [23–25]. A large aperture scintillometer (LAS) can measure the path-averaged C_n^2 within a certain distance in high time resolution, which is also a common instrument using the intensity scintillation principle [26–28].

Moreover, by adjusting the focal length and remaining at each height to reduce the variance of the distribution of lidar profiles, imaging methods that use the differential image motion monitor (DIMM) are effective methods for detecting turbulence intensity profiles [29–35]. Using atmospheric backscattering amplification phenomena by measuring the intensity of laser echo signal amplification effects can also calculate C_n^2 under certain conditions [36–38].

However, there are some limitations with respect to these methods in effectively detecting rapidly changing atmospheric turbulence within its integral length scale and time scale. For example, it normally takes a long period of time when using balloon methods; the optical scintillation becomes saturation when detecting long distances; it is difficult for imaging methods to improve spatial resolution; the response to temperature fluctuation is not sensitive enough using the Raman lidar [39]. Consequently, it is necessary to seek a method that can detect turbulence profiles with high temporal and spatial resolution simultaneously.

Coherent Doppler wind lidar (CDWL) obtains radial wind speed information by retrieving the frequency shift of the received signal after passing through a distance in the atmosphere [40–42]. Its reliable performance has been verified in various areas, such as the following: turbulence parameters [43–47], aircraft wake vortices [48], boundary layer height [49–51], cloud seeding [52], gravity waves [53,54], low-level jets (LLJs) [44,55,56], simultaneous wind and rainfall detection [57], identifying different atmospheric environments [58], and others [59,60]. Therefore, using CDWL is a promising method for detecting the dynamic part of turbulence with high resolution.

A microwave radiometer (MWR) can provide profiles of temperature, water vapor density, relative humidity, etc. [61], which supplement the thermodynamics part of turbulence for C_n^2 retrieval. Consequently, C_n^2 profiling with high temporal and spatial resolution can be achieved by using a combination of CDWL and MWR.

This paper begins with a principle to estimate C_n^2 in Section 2. In Section 3, a horizontal comparison experiment with LAS is carried out firstly. The results of different methods are discussed. The limitation and its uncertainty are analyzed next. Then, the continuous observation results of C_n^2 profiles are retrieved vertically. Later, several turbulence parameters such as the buoyancy term, gradient Richardson number, perturbations of temperature and wind, variance of the fluctuations of vertical wind, and flux of potential temperature are estimated to analyze turbulence characteristics. After that, five typical sets of 12 min continuous turbulent profiles representing different periods of daytime and night-time are analyzed and compared with the turbulence model. The uncertainty of this method is also calculated in the vertical experiment. Finally, conclusions and discussion are provided in Section 4.

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2. Principle

2.1. Stable Stratification

In the "inertial sub-region" (between inner scale l_0 and outer scale L_0), where the refractive index structure function obeys the Kolmogorov "2/3 law" ($D_n(r) = C_n^2 r^{2/3}$) [62], turbulent energy propagates from the outer scale to the inner scale without dissipation. According to Tatarskii's theory [63], under stable stratification, by combining wind field data or the outer scale of turbulence L_0 with meteorological parameters, C_n^2 can be calculated by Equation (1) [64]:

$$C_n^2 = a^2 \times \left[\frac{K_m^2}{\left(\frac{\partial \vec{U}}{\partial z}\right)^2} \right]^{1/3} \times M^2 = a^2 L_0^{4/3} M^2$$
 (1)

where a^2 is a constant, usually takes the experimental empirical value of 2.8, and M is the vertical gradient of generalized potential refractive index. K_m is the eddy viscosity (coefficient of mixing of momentum), and $\partial U/\partial z$ is the wind shear of the horizontal wind vector in the vertical direction. In the latter method, the calculation of L_0 is quite difficult. Usually, it is estimated by different outer scale models [65,66] based on Tatarskii's theory, such as the Colman–Vernin (C-V) model [66], which expresses L_0 as a function of altitude only within 2–17 km. Moreover, the Dewan model [67] considers the effect of both altitude and wind shear of the horizontal wind, which has different expressions in the troposphere and stratosphere of the following:

$$L_0^{4/3}(z) = \begin{cases} 0.1^{4/3} \times 10^{1.64 + 42 \times S(z)}, troposphere \\ 0.1^{4/3} \times 10^{0.506 + 50 \times S(z)}, stratosphere \end{cases}$$
(2)

where z is the height (m), and S(z) is the intensity of the wind shear.

Most of these models are related to height, wind shear intensity, and temperature gradient. Empirical models are normally obtained from long-term statistical averaged data with an in situ sounding balloon, which is hard for reflecting local atmospheric features in different areas. In addition, wind shear and temperature gradient cannot be measured directly, and they are closely related to the scale chosen for calculation. It would be more robust when choosing a larger scale, but it might lose detailed messages and would be more sensitive on the contrary. In order to reduce errors, it is necessary to avoid using these parameters for calculation as much as possible.

Therefore, the former part of Equation (1) is mainly discussed and adopted in this paper under stable stratification conditions. From the simplified turbulence kinetic energy (*TKE*) budget equation for steady states, the following expression is described [68]:

$$\frac{d(TKE)}{dt} = \underbrace{\left(-\langle u'w'\rangle \frac{\partial \vec{u}}{\partial z} - \langle v'w'\rangle \frac{\partial \vec{v}}{\partial z}\right)}_{I} + \underbrace{\frac{g}{\Theta}\langle w'\theta'\rangle}_{II} - \varepsilon = 0 \tag{3}$$

Term I is a positive contribution to TKE caused by wind shear, where u', v', and w' are fluctuations of the wind component in zonal, meridional, and vertical directions. Term II is the buoyant production or consumption term depending on the sign of the vertical heat flux (positive during the daytime or negative at night). Here, g denotes gravity acceleration, and Θ is the averaged potential temperature. θ' is the fluctuation of potential temperature. The angle bracket means spatial average. Finally, ε is the turbulent kinetic energy dissipation rate (TKEDR), which is always a loss term.

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When using the K-theory, the vertical flux of a turbulent scale quantity can be related to its local mean gradient [68]. Then, the fluxes of wind component and potential temperature have the following expression:

$$\langle u'w'\rangle = -K_m \frac{\partial \overrightarrow{u}}{\partial z} \tag{4}$$

$$\langle v'w'\rangle = -K_m \frac{\partial \overrightarrow{v}}{\partial z} \tag{5}$$

$$\langle w'\theta' \rangle = -K_{\theta} \frac{\partial \Theta}{\partial z} \tag{6}$$

where K_{θ} is the coefficient of mixing of heat. Therefore, combining Equations (3)–(6), ε can be rewritten as follows:

$$\varepsilon = K_m S^2 - K_\theta N^2 \tag{7}$$

where $S = \partial \overrightarrow{U}/\partial z$, which can be calculated by the following equation:

$$S^{2} = \left(\frac{\partial \overrightarrow{u}}{\partial z}\right)^{2} + \left(\frac{\partial \overrightarrow{v}}{\partial z}\right)^{2} \tag{8}$$

and N^2 is the square of the buoyancy frequency.

$$N^2 = \frac{g}{\Theta} \left(\frac{\partial \Theta}{\partial z} \right) \tag{9}$$

Then, by using the relationship between K_m and K_{θ} , Equation (7) has a new expression of the following [69]:

$$\varepsilon = K_m S^2 \left(1 - \alpha N^2 / S^2 \right) = K_m S^2 \left(1 - \alpha R_g \right) \tag{10}$$

where $\alpha = K_{\theta}/K_m$ ($Pr_t = \alpha^{-1}$ is the turbulent Prandtl number) and $R_g = N^2/S^2$ is the gradient Richardson number. From the definition, one can see that the Rr_t is an indicator of discrepancy between turbulent transport by heat and momentum. With gradient Richardson number R_g and flux Richardson number R_f , Rr_t can be shown as follows:

$$Pr_t = \frac{R_g}{R_f} \tag{11}$$

Under stable conditions, Rr_t grows nearly linear with increasing R_g and has an empirical function of the following [70–72]:

$$Pr_{t} = Pr_{t}^{neu} \exp\left(-\frac{R_{g}}{Pr_{t}^{neu}R_{f}^{max}} + \frac{R_{g}}{Pr_{t}^{neu}}\right) + \frac{R_{g}}{R_{f}^{max}}$$
(12)

where $Pr_t^{neu} = 0.8$ is the turbulent Prandtl number under neutral conditions. $R_f^{max} = 0.25$ is the maximum flux Richardson number.

Next, substituting Equation (10) into Equation (1) yields the following:

$$C_{n \ Tatarskii,1961}^2 = a^2 \times \frac{\left(\frac{\varepsilon}{1 - \alpha R_g}\right)^{2/3}}{S^2} \times M^2$$
 (13)

From Equation (13), one can find that the result of C_n^2 is affected by both dynamics and thermodynamics. In addition, ε can be calculated by matching the measured radial velocity

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and azimuth structure function with the theoretical structure function [56]. Moreover, *M* has the expression of the following [63]:

$$M = -79 \times 10^{-6} \left(\frac{P}{T}\right) \left[\frac{\partial \ln \theta}{\partial z} + \frac{15,500q}{T} \left(\frac{\partial \ln \theta}{\partial z} - \frac{1}{2q} \frac{dq}{dz} \right) \right]$$
(14)

where *q* is the specific humidity (g/g), and θ is the potential temperature:

$$\theta = T(\frac{1000}{P})^{0.286} \tag{15}$$

where *T* represents temperature (K). *P* means pressure (hPa). However, since humidity contributions are expected to be insignificant in the optical range [69], parameter *M* for dry air can be rewritten as follows [67]:

$$M = -79 \times 10^{-6} \frac{P}{T} \left(\frac{\partial \ln \theta}{\partial z} \right) \tag{16}$$

In order to simplify the calculation and analyze the effects of temperature and pressure gradients, merging Equations (15) and (16) yields the following:

$$M = -79 \times 10^{-6} \frac{P}{T} \left(\frac{1}{T} \frac{dT}{dz} - \frac{0.286}{P} \frac{dP}{dz} \right)$$
 (17)

If the hydrostatic hypothesis is used and pressure data are unavailable, $\partial \ln \theta / \partial z$ can be simplified into the following [73]:

$$\frac{\partial \ln \theta}{\partial z} = \frac{1}{T} \left(\frac{dT}{dz} + \frac{g}{C_v} \right) \tag{18}$$

where $C_p = 1004 \, \text{JKg}^{-1} \text{K}^{-1}$.

From Equation (13) to Equation (18), one can see that, with the TKEDR and wind profiles measured from CDWL in the inertial subrange and temperature and pressure profiles derived from MWR and the barometric formula, the refractive index structure constant C_n^2 can be estimated under stable stratification circumstances.

2.2. Convective Boundary Layer

When temperature stratification is unstable under the convective boundary layer (CBL), especially within the well-mixed part (0.2 \sim 0.8 z/z_i , where z_i is the height of CBL), the source of turbulence becomes mainly buoyancy-driven. Then, due to the non-local large-eddy heat flux, Equations (4)–(6) and (10) that are based on K- theory failed to deal with the "zero/counter-gradient" region, where $\partial\Theta/\partial z \geq 0$ while $\langle w'\theta' \rangle > 0$ [68,74]. Likewise, temperature structure constant C_T^2 and refractive index structure constant C_n^2 are not proportional to $(dT/dz)^2$ and M^2 anymore. Therefore, C_n^2 should not be calculated with Equation (13) within CBL.

In the optical range, structure characteristics C_n^2 and C_T^2 are related by the following equation:

$$C_n^2 = \left(\frac{79 \times 10^{-6} P}{T^2}\right)^2 C_T^2 \tag{19}$$

In the surface layer and lower portion of CBL, where $\varepsilon(z)$ is approximately a constant and $C_T^2(z)$ decreases with $z^{4/3}$, C_T^2 can be estimated by the following [69]:

$$C_T^2 = \frac{a^2 C_1}{3\alpha \kappa^{4/3}} \frac{\varepsilon^{4/3}}{\beta^2 z^{4/3}}$$
 (20)

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where C_1 is a constant, κ is the von Kármán's constant, β is a dimensional parameter ($\beta = g/\Theta$), and all the rest are the same as before. The entire numerical coefficient is found to be around 0.7; thus, the equation can be rewritten as follows:

$$C_{T \ Tatarskii,1971}^2 = \frac{0.7}{\beta^2} \left(\frac{\varepsilon}{z}\right)^{4/3} \tag{21}$$

Accordingly, C_n^2 in the near-surface layer has the following expression:

$$C_{n\ Tatarskii,1971}^{2} = \left(\frac{79 \times 10^{-6}P}{T^{2}}\right)^{2} \frac{0.7}{\beta^{2}} \left(\frac{\varepsilon}{z}\right)^{4/3}$$
 (22)

In addition, to correct Equation (6) in the well-mixed area of CBL, a positive "countergradient term" γ_C is provided and Equation (6) becomes the following [74,75]:

$$\langle w'\theta' \rangle = -K_{\theta} \left(\frac{\partial \Theta}{\partial z} - \gamma_C \right)$$
 (23)

One commonly used expression of γ_C is as follows:

$$\gamma_{\rm C} = \frac{g}{\Theta} \frac{\langle w'^2 \rangle}{\langle \theta'^2 \rangle} \tag{24}$$

where $\langle w'^2 \rangle$ and $\langle \theta'^2 \rangle$ are the variances of the fluctuations of the vertical wind component and potential temperature. Then, temperature structure constant C_T^2 can be estimated from γ_C and ε [76].

$$C_{T\ Luce,2020}^2 = \frac{\varepsilon^{2/3} \gamma_C}{0.36} \frac{\Theta}{g}$$
 (25)

Substituting Equation (25) into Equation (19) yields the following:

$$C_{n\ Luce,2020}^{2} = \left(\frac{79 \times 10^{-6} P}{T^{2}}\right)^{2} \frac{\varepsilon^{2/3} \gamma_{C}}{0.36} \frac{\Theta}{g}$$
 (26)

Therefore, C_n^2 in the near-surface (0 ~ 0.2 z/z_i) and well-mixed (0.2 ~ 0.8 z/z_i) part of CBL can be estimated with Equations (22) and (26), respectively. The area above 0.8 z/z_i of CBL and under the conditions of stable stratification is then calculated with Equation (13).

3. Experiments

A horizontal verification experiment is carried out on the University of Science and Technology of China (USTC) campus in Hefei City, Anhui Province (31°50′10″N, 117°16′10″E), to discover a suitable method for C_n^2 retrieval. After that, the vertical field experiment is conducted on the Xilin Gol Prairie in Inner Mongolia (43°54′N, 115°58′E) to test the behavior of this method in C_n^2 profiling. The two experimental sites are shown on the left of Figure 1.

3.1. Instruments

The CDWL applied in this paper (Site A of Figure 1, right.) uses an eye-safe 1.55 μm wavelength in the transmitting system, the single pulse energy of the laser is 200 μJ , and repetition frequency is 10 kHz. In the experiment, CDWL adopts a velocity azimuth display (VAD) scanning mode, and the elevation angle is fixed at 60 degrees. The step length of the scanning azimuth angle is 5 degrees, and the scanning period is 147 s, which is the same as the temporal resolution of the retrieved wind field.

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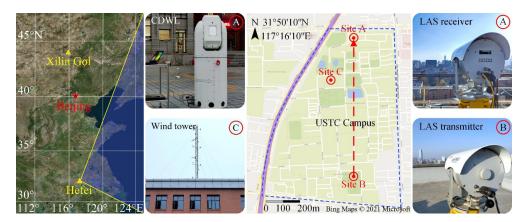


Figure 1. Illustration of two experiment sites in the satellite map and the instruments layout in the horizontal experiment (USTC, Hefei City).

The lidar has a pulse width of 200 ns, which has a blind zone of around 30 m. Thus, in the vertical direction of 0.03–2.20 km, 2.20–4.79 km, and 4.79–11.29 km, the spatial resolutions are 30 m, 60 m, and 150 m, respectively. In addition, lidar adopts an all-fiber structure and temperature control system in order to ensure stability. The specific parameters of CDWL are listed in Table 1.

Table 1. Key Parameters of CDWL.

Parameter	Value	
Wavelength	1548 nm	
Pulse energy	200 μJ	
Pulse width	200 ns	
Repetition frequency	10 kHz	
Temporal resolution	2 s	
Azimuth scanning range	0–360°	
Zenith scanning range	0–90°	

The ground-based MWR used in the experiment has a time resolution of 2 min. In the vertical direction of 0–0.5 km, 0.5–2 km, and 2–10 km, the spatial resolution is as follows: 50 m, 100 m, and 250 m, respectively. Ground surface measurements contain temperature, humidity, pressure, and cloud base height, and vertical observation results can provide profiles of temperature, water vapor density, relative humidity, and liquid water content within 0–10 km. There are more specific introductions and applications about MWR in [61].

Under the assumption of horizontally homogeneous, LAS (Kipp&Zonen LAS MKII, Figure 1, right.) can retrieve path-averaged C_n^2 by detecting the light intensity fluctuations of signals in the receiving end that pass through a distance in the atmosphere. LAS was chosen for the verification experiment due to its mature theory and reliable results. It can provide C_n^2 information at a temporal resolution of 1 s. In this experiment, a 10 min time interval is adopted to reduce data fluctuations.

3.2. Verification Experiment

In the horizontal direction verification experiment, as shown in the right of Figure 1, CDWL and the weather station (DAVIS6162: Wireless Vantage Pro2 Plus [77]) are placed at site A. The receiving and transmitting ends of LAS are located at the height of 55 m at site A and site B, respectively. Its detection path (in the direction of the red arrow) is a southnorth direction in order to avoid the influence of sunlight. The two sites are 900 m apart, which is within the best detection range of LAS to avoid scintillation saturation or aperture averaging effects [78]. The wind tower is placed on the top of a 6-story building about 30 m high at site C to record the continuous data of temperature and for the calculation of temperature gradient.

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As shown in Figure 2, six days of continuous observations were carried out from 00:00 on 26 September to 24:00 on 1 October 2020, local time. Figure 2a–e represent wind field and TKEDR results obtained from the CDWL, Figure 2f is the temperature data recorded at the height of 2 m, 8 m, and 18 m of the wind tower and the temperature gradient result calculated by linear fitting. Figure 2g shows the variances of vertical wind component fluctuation and the heat flux of potential temperature. The results of $\log_{10}C_n^2$ that are estimated by different methods introduced in the principle part are drawn in Figure 2h. Since the height of the wind tower is about 18 m and near the ground, which represents the changes in a local area of the surface, the calculated temperature gradient can vary widely every day. In addition, the method used to estimate $C_{n\ Tatarskii,1961}^2$ is suitable for stable conditions. Therefore, to reduce errors, in the process of calculating $C_{n\ Tatarskii,1961}^2$ in the horizontal experiment, the temperature gradient is taken as the empirical value in the troposphere: $-0.0065\ \text{K/m}$; the pressure gradient is $-0.10\ \text{hPa/m}$.

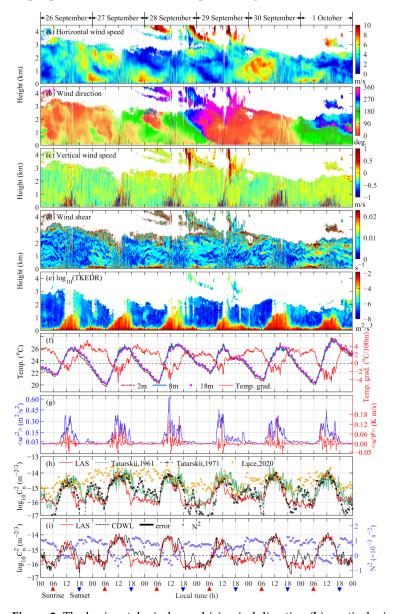


Figure 2. The horizontal wind speed (a), wind direction (b), vertical wind speed (c), wind shear (d), $\log_{10}(\text{TKEDR})$ (e), temperature and its gradient (f), variances in vertical wind fluctuation and flux of potential temperature (g), $\log_{10}C_n^2$ estimated by different methods (h), Brunt–Väisälä frequency squared, $\log_{10}C_n^2$ and its shaded area error bar (i) retrieved from CDWL, wind tower, and LAS in the observations from 26 September to 1 October 2020, local time.

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Combining with the daily trend of the temperature gradient in Figure 2f, it can be observed that it has a strong negative correlation with the C_n^2 result detected by LAS and the temperature gradient. Obviously, there is a strong temperature inversion in the surface layer from afternoon to night every day. On the one hand, when the temperature gradient changes from negative to positive around 16:00 in the afternoon, the convection activities weaken instantly and C_n^2 drops rapidly [79,80]. It can also be verified from the vertical wind speed in Figure 2c that it becomes more stable and approaches zero when temperature inversion develops.

On the other hand, with an increase in temperature gradient, a stratified structure begins to form. This can be proved by the Brunt–Väisälä frequency, which is a common method for estimating the stability of atmosphere stratification [53,81–83] (Equation (9)). When $N^2>0$, the stratification structure is stable, and it becomes unstable when $N^2<0$ due to the inversion of density. The continuous time profile of N^2 calculated from the wind tower is shown in Figure 2i. It can be found that N^2 also turns from negative to positive after around 16:00, similarly to the temperature gradient, which means that atmosphere stratification becomes more stable and the laminar flow grows.

LLJs can often be found at the night, especially on 26, 27, and 30 September. The occurrence of low-level jet (LLJ) usually leads to an increase in wind shear, which in turn breaks the stability of the atmosphere and generates turbulent flow. However, unlike the daytime, the increase in wind shear did not cause a wide range of turbulence due to the suppressing effect of the Brunt–Väisälä frequency. Instead, only small fluctuations occurred on the edge of LLJ, which can be found in the slight variations of C_n^2 at night.

In addition, from the discrepancy of C_n^2 estimated by different methods (Figure 2h), some interesting phenomena can be found. When the variances of vertical wind fluctuation $\langle w'^2 \rangle$ is neglectable at night-time, the flux of potential temperature $\langle w'\theta' \rangle$ is also near zero due to the lack of vertical motion. While during the daytime, with the increase in convective activities driven by surface heating, the potential temperature heat flux becomes positive (meaning upwards). At the same time, the temperature gradient and corresponding N^2 drop to near zero and can even approach negative values. Thus, the method derived from stable stratification is no longer applicable. It can be proved from the $C_{n\ Tatarskii,1961}^2$ shown in Figure 2h that it becomes unstable and fluctuates around 1–2 orders of magnitude during these periods.

The result of $C_{n\ Tatarskii,1971}^2$ that applies to the surface layer and lower portion of CBL shows a fine consistency with LAS during the daytime. Moreover, it is normally underestimated during the nighttime due to the decline of temperature and TKEDR.

Similarly, the method for estimating $C_{n\ Luce,2020}^2$ is mainly suitable for the well-mixed area of CBL during the daytime; thus, the restrictions for using this method in near-surface detection are stricter. For the rest of the time when temperature stratifications are stable, $C_{n\ Luce,2020}^2$ is able to overestimate results from the small variances of potential temperature fluctuations.

Therefore, considering the limitations of different methods, a combination of them should be applied for continuous C_n^2 retrieval. In our horizontal near-surface experiment, the method for estimating $C_{n\ Tatarskii,1961}^2$ is mostly adopted before sunrise and after sunset. After sunrise, $C_{n\ Tatarskii,1971}^2$ is used due to the variance of vertical wind fluctuation over a threshold value ($\langle w'^2 \rangle \geq 0.03\ \text{m}^2/\text{s}^2$ is taken in this paper). If $\langle w'^2 \rangle \geq 0.03\ \text{m}^2/\text{s}^2$ is still satisfied after sunset, then this method is used until $\langle w'^2 \rangle$ is smaller than $0.03\ \text{m}^2/\text{s}^2$. The combination of these methods and its comparison with LAS are shown in Figure 2i.

The statistical analyses of the results in six-day continuous observations from LAS and CDWL are shown in Figure 3c. The results of $C_{n\ Tatarskii,1961}^2$ and $C_{n\ Tatarskii,1971}^2$ are plotted in black dots and green circles, respectively. By comparing the orders of magnitude of C_{n}^{2} , one can find that their results are quite consistent every day.

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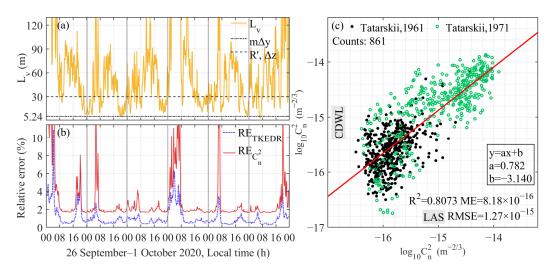


Figure 3. The integral scale L_v (a), relative error of the estimation of TKEDR and C_n^2 (b), and comparative statistical analysis of LAS and CDWL observation results (c) from 26 September to 1 October 2020, local time.

The $C_{n\ Tatarskii,1961}^2$ that conducted estimations during nighttime is mainly distributed around $10^{-16}\ \mathrm{m}^{-2/3}$ and $C_{n\ Tatarskii,1971}^2$ and within $10^{-15}\ \mathrm{to}\ 10^{-14}\ \mathrm{m}^{-2/3}$ during the daytime. The correlation coefficient, mean error, and standard deviation RMSE between the new combination method and LAS are 0.8073, $8.18\times10^{-16}\ \mathrm{m}^{-2/3}$, and $1.27\times10^{-15}\ \mathrm{m}^{-2/3}$, respectively.

3.3. Limitation and Uncertainty Analysis

To make this new method more practical and convincing, testifying the applicability and estimating its uncertainty under different circumstances are significant procedures.

Integral scale L_v is an indicator reflecting the rationality of the turbulence parameters retrieval [46]. The Kolmogorov "2/3 law" holds, and the lidar measurement is within an inertial subrange when the longitudinal and transverse dimensions of the sensing volume do not exceed the upper boundary of the inertial subrange ($L_v > \max\{\Delta y, \Delta z\}$, Δy is the spatial distance between the centers of two neighbouring probing volumes, Δz is the longitudinal dimension of the probing volume, and $\Delta z = 30$ m and 60 m in the vertical direction of 0.03–2.20 km and 2.20–4.79 km, respectively). It can be calculated from the radial velocity variance averaged over all azimuth angles (\overline{c}_r^2) and TKEDR [84]:

$$L_v = \frac{0.698 \left(\overline{\sigma}_r^2\right)^{3/2}}{\varepsilon} \tag{27}$$

where $\overline{\sigma}_r^2$ has the following expression:

$$\overline{\sigma}_r^2 = (\sin\varphi)^2 \sigma_w^2 + \left(\frac{1}{2}\right) (\cos\varphi)^2 \left(\sigma_u^2 + \sigma_v^2\right) \tag{28}$$

where $\varphi=60^\circ$, $\sigma_u^2=<(u')^2>$, $\sigma_v^2=<(v')^2>$, and $\sigma_w^2=<(w')^2>$ are the variances of the fluctuations of zonal, meridional, and vertical wind components. On the one hand, when distance $l\Delta y < L_v$ is additionally satisfied ($l\Delta y=5.24$ m in the horizontal experiment and grows with height in the vertical observation), it indicates that TKEDR can be obtained within the inertial subregion of turbulence. Normally, $\max\{\Delta y, \Delta z\}$ is smaller than $m\Delta y$, especially in the vertical measurement (in our experiment setup, $l\Delta y>\max\{\Delta y,\Delta z\}$ holds when the height is above 297.7 m). On the other hand, if the radius of the scanning cone at a certain height R' (R'=30 m at the height of 60 m and grows with height in the vertical observation) is comparable with or is smaller than L_v , the relative error of estimation of TKEDR (RE_{TKEDR}) becomes larger.

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From the results of L_v in Figure 3a, one can observe that it is bigger than Δy , Δz , and $l\Delta y$ in most cases, which means that TKEDR and C_n^2 are measured and retrieved within the inertial subrange most of the time during the experiment. During the transition period around 16:00–20:00, the integral scale of turbulence L_v drops to the scale smaller than Δz . Similarly to the results shown in the temperature gradient and N^2 , this verified the prominent motion state of atmosphere changes from convective to laminar flow and the sensing volume exceeding the integral scale of turbulence. Thus, the spatial resolution of CDWL Δz needs to be improved in near-surface observations in future studies. In addition, the results also indicate that it is reliable to use the $L_v > \max\{\Delta y, \Delta z\}$ criterion in measuring the credibility of the new method.

To estimate the relative error of C_n^2 , the method for calculating TKEDR should be explained first because it is a key parameter in C_n^2 retrieval. When using CDWL to estimate the wind field, the averaged azimuth structure function has the following expression [43,84]:

$$\overline{D}_{L}(l\Delta\theta) = \frac{1}{N} \sum_{n=1}^{N} \frac{1}{M-l} \sum_{m=1}^{M-l} \left[V_{r}'(R_{k}, \theta_{m} + l\Delta\theta, n) - V_{r}'(R_{k}, \theta_{m}, n) \right]^{2}$$
(29)

where $n=1, 2, 3, \ldots, N$ is the number of conical scans used for averaging, and M is the number of radial velocity estimates in one conical scan. $V'_r = V_L - \langle V_L \rangle$ describes the fluctuations of radial velocity, with R_k being the distance from the lidar to the center of the sensing volume, $\theta_m = m\Delta\theta$ is the azimuth angle, and $\Delta\theta$ is the azimuth angle resolution. $l=1, 2, 3, \ldots, L$ and $L\Delta\theta \ll \pi/2$. In addition, function $A(l\Delta y_k)$ can be expressed as follows:

$$A(l\Delta y_k) = 2\int_0^\infty d\kappa_1 \int_0^\infty d\kappa_2 \Phi(\kappa_1, \kappa_2) H_{\parallel}(\kappa_1) H_{\perp}(\kappa_2) [1 - \cos(2\pi l \Delta y_k \kappa_2)]$$
 (30)

where the following is obtained.

$$\Phi(\kappa_1, \kappa_2) = 0.0652(\kappa_1^2 + \kappa_2^2)^{-\frac{4}{3}} \left[1 + (8/3)\kappa_2^2 / \left(\kappa_1^2 + \kappa_2^2\right) \right]$$
(31)

 $H_{\parallel}(\kappa_1) = \left[\exp\left\{-(\pi\Delta p\kappa_1)^2\right\}\sin c(\pi\Delta R\kappa_1)\right]^2$ is the longitudinal transfer function of the low-pass filter, and $H_{\perp}(\kappa_2) = \left[\sin c(\pi\Delta y_k\kappa_2)\right]^2$ is the transverse transfer function of the low-pass filter. $\sin c(x) = \sin x/x$, $\Delta p = c\sigma_p/2$, $\sigma_p = \tau_p/\left(2\sqrt{\ln 2}\right)$, and τ_p is the pulse duration. $\Delta R = cT_W/2$, c is the speed of light, and T_W is the temporal window width. $\Delta y_k = \Delta\theta R_k \cos\varphi$ is the transverse size of the sensing volume.

With the equation of $\overline{D}_a(l\Delta\theta) = \varepsilon^{2/3}A(l\Delta\theta)$, the difference of $\overline{D}_L(l\Delta\theta) - \overline{D}_L(\Delta\theta)$ is equal to $\overline{D}_a(l\Delta\theta) - \overline{D}_a(\Delta\theta)$. Then, ε can be obtained from the difference of the averaged azimuth structure function of radial velocity.

$$\varepsilon = \left[\frac{\overline{D}_L(l\Delta\theta) - \overline{D}_L(\Delta\theta)}{A(l\Delta y_k) - A(\Delta y_k)} \right]^{3/2}$$
(32)

Next, the relative error of the estimation of C_n^2 ($RE_{C_n^2}$, in real value, rather than logarithmic scale) is calculated according to Equations (13), (22), and (26) as follows:

$$RE_{C_{nTatarski,1961}^{2}} = \left\{ \frac{4}{9} \left[(RE_{TKEDR})^{2} + \left(RE_{1-\alpha R_{g}} \right)^{2} \right] + 4 \left[(RE_{windshear})^{2} + \left(RE_{M(T,P)} \right)^{2} \right] \right\}^{1/2}$$
(33)

where RE_{TKEDR} is estimated based on lidar system parameters, the value of TKEDR, and the instrumental error of the radial velocity (σ_e) [43,84]. σ_e is mainly affected by CNR, and it is calculated by the model of Cramer–Rao lower bound (CRLB) with an

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assumption of a Gaussian laser pulse [85–87]. The expression of $1-\alpha R_g$ is complicated (Equations (11)–(12)); nonetheless, it has asymptotical behaviors (close to 0.75) when $R_g>1$. Thus, the uncertainty caused by $RE_{1-\alpha R_i}$ is relatively small considering that it is used in stable stratification (takes ± 0.01 at 0.75 here). $RE_{windshear}$ can be derived from the sum of the relative error of horizontal wind in different altitudes divided by the distance between two layers. According to Equation (17), $RE_{M(T,P)}$ is estimated by the relative error of temperature (RE_T) and pressure (RE_P). In this paper, RE_T takes ± 1 K at 280 K and RE_P takes ± 1 hPa at 800 hPa.

When using Equation (22) to estimate $C_{n \; Tatarskii,1971}^2$, we obtain the following:

$$RE_{C_{n \text{ Tatarskii,1971}}^{2}} = \left[4(RE_{P})^{2} + 16(RE_{T})^{2} + \frac{16}{9}(RE_{TKEDR})^{2} + 4(RE_{\Theta})^{2}\right]^{1/2}$$
(34)

and when $C_{n\ Luce,2020}^2$ is adopted, the following is obtained.

$$RE_{c_{nLuce,2020}^{2}} = \left[4(RE_{P})^{2} + 16(RE_{T})^{2} + \frac{4}{9}(RE_{TKEDR})^{2} + \left(RE_{\langle\theta'^{2}\rangle}\right)^{2} + \left(RE_{\langle w'^{2}\rangle}\right)^{2}\right]^{1/2}$$
(35)

Finally, $RE_{C_n^2}$ is calculated by using the same combination method as C_n^2 in Figure 2i. The six-day continuous results of RE_{TKEDR} and $RE_{C_n^2}$ are plotted in Figure 3b. Since the height in the horizontal experiment is near the surface layer, CNR is high and the instrumental error of estimation of the wind field is quite small. Therefore, the relative errors of TKEDR and C_n^2 are within 10% most of the time, which demonstrates the robustness of this method. $RE_{C_n^2}$ is also shown in Figure 2i with a shaded area error bar. Since C_n^2 is usually pictured on a log scale, a 10% relative error is not obvious in the figure.

3.4. Continuous Observation of C_n^2 Profile

Based on the results of the horizontal verification experiment, the results of the continuous field experiment conducted on the Xilin Gol Prairie in Inner Mongolia (43°54′N, 115°58′E) in September 2019 are analyzed and discussed. Different from cities, the topography of the grassland makes the atmosphere in CBL more likely to meet homogeneous assumptions.

Figure 4a–c,e–g show the wind field and TKEDR results retrieved from CDWL in two continuous days from 10:00 on 6 September to 24:00 on 7 September 2019, local time. The quality of data is affected by carrier-to-noise (CNR), which is the ratio of total signal power to the noise power, and it is the main parameter that determines the accuracy of wind field retrieval. In this paper, the data with CNR above -35 dB were selected for retrieving radial wind speed [59]. Due to the effect of turbulence, the boundary layer height is uplifted during the daytime; thus, CNR can be detected at higher values accordingly. A sudden increase in CNR above 2.2 km is caused by a change in spatial resolution (Figure 4a during the nighttime). In addition, the horizontal wind direction defines the north wind as 0° and the degree increases in the clockwise direction.

Similarly to the results observed in the horizontal verification experiment, the fluctuations of horizontal wind speed and direction remain small, and vertical motion is neglectable mostly at night except for an LLJ that can be discovered around 0.6 km (Figure 4b). Therefore, the stratification of the atmosphere is stable at nighttime. After sunrise, when the air is warmed and the ground is unevenly heated, convection activities begin to occur. This can be verified from the vertical wind speeds, which differ from the stable state that approaches zero most of the time during the night, and it changes quickly between positive and negative numbers (negative means upward). The stable stratification structure and LLJ that occurred at night also gradually vanished, as shown in the horizontal wind speed and wind direction during the day. Correspondingly, the calculated horizontal wind shear is smaller compared with those observed during nighttime.

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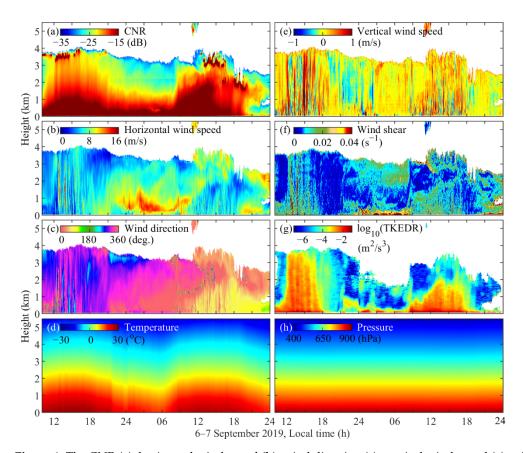


Figure 4. The CNR (a), horizontal wind speed (b), wind direction (c), vertical wind speed (e), wind shear (f), and log₁₀(TKEDR) (g) derived from CDWL. The temperature (d) and pressure (h) retrieved from MWR and the barometric formula in the observations from 6 September to 7 September 2019, local time.

The results of temperature and pressure profiles in 0–5 km derived from MWR are shown in Figure 4d,h. Obviously diurnal variations can be observed from the continuous results of the temperature profile. It should be mentioned that because MWR does not have pressure profile data, considering that atmospheric pressure normally decreases monotonously and rapidly with height, we used the barometric formula to calculate the pressure profile under the assumption that the temperature gradient is constant within a certain height range. The pressure in the height of h_i can be derived by using the following equation:

$$P_{i} = P_{i-1} \left(1 - \frac{k(h_{i} - h_{i-1})}{T_{i-1}} \right)^{\frac{gM}{Rk}}$$
(36)

where T_{i-1} and P_{i-1} are the temperature (K) and pressure (hPa) in h_{i-1} , respectively. k is the temperature gradient (K/m) between the height of h_i and h_{i-1} ; g is gravitational acceleration (9.8 m/s²); M is the molar mass of Earth's air (0.029 kg/mol); R is the universal gas constant (8.314 J/(mol·K)). Using the temperature profile measured by MWR and the recorded surface pressure, the pressure profile can be calculated from the bottom (the experimental site is 1160 m above sea level) to the top by using the differential method.

Then, according to wind field information derived from CDWL and meteorological data recorded by MWR, two-day continuous observation results of C_n^2 profiles can be retrieved by using different methods, as shown in Figure 5c–e. The variances in the fluctuations of vertical wind component $\langle w'^2 \rangle$ and the instantaneous vertical flux of potential temperature $w'\theta'$ are also drawn here for comparison (Figure 5a,b).

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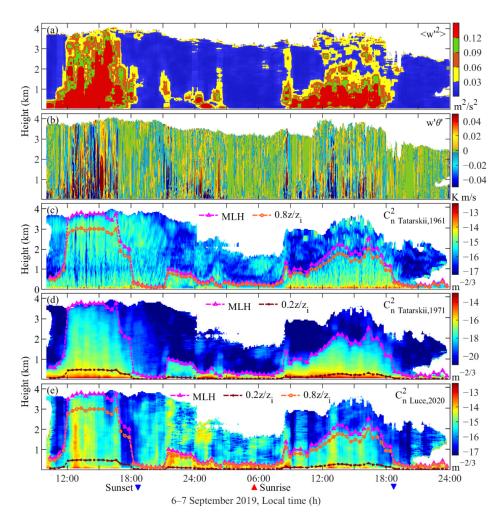


Figure 5. The results of the variances of vertical wind fluctuation (**a**), instantaneous flux of potential temperature (**b**), $\log_{10}C_n^2$ estimated by $C_{n\ Tatarskii,1961}^2$ (**c**), $C_{n\ Tatarskii,1971}^2$ (**d**), and $C_{n\ Luce,2020}^2$ (**e**) in the observations from 6 September to 7 September 2019, local time.

Considering that the threshold value of $\langle w'^2 \rangle$ is taken as 0.03 m²/s² in the horizontal experiment, an area with $\langle w'^2 \rangle < 0.03$ m²/s² is depicted in blue. Clearly, after sunset and before sunrise, $\langle w'^2 \rangle$ is smaller than 0.03 m²/s² most of the time except for the area around LLJ (Figure 4b). Thus, atmospheric stratification can be assumed as stable overall during the night-time. In addition, the heat flux of the potential temperature that is mainly close to zero can also prove this observation. In order to compare with CBL, the mixing layer heights (MLHs) are also drawn here using a threshold method of $\varepsilon < 10^{-4}$ m²/s³ [45,51]. On the contrary, $\langle w'^2 \rangle \geq 0.03$ m²/s² holds throughout the daytime, especially under CBL. Moreover, the well-mixed part is mainly within 0.2 ~ 0.8 z/z_i. Meanwhile, from Figure 5b, one can observe that $w'\theta'$ is normally larger than zero under 0.8 z/z_i due to the surface heating effect, and it becomes negative in the entrainment zone (>0.8 z/z_i).

From the result of C_n^2 $_{Tatarskii,1961}$ (Figure 5c), some layer structures can be found above CBL, especially after sunset. However, when dealing within CBL during the daytime, it can fluctuate quickly about 1–2 orders of magnitude with both time (6 September) and height (7 September), as revealed in the horizontal experiment (Figure 2h). Moreover, there is a sudden decreasing layer at around 1 km that can be found in C_n^2 $_{Tatarskii,1961}$ during the daytime on 6 September. The reason for these phenomena can be analyzed by using Equations (13) and (16). The gradient terms can become unstable when wind shear fluctuates quickly (Figure 4f) and the potential temperature gradient $d\Theta/dz$ drops to zero and can even approach negative values in the well-mixed region. Therefore, this method is not suitable for C_n^2 retrieval when stratification is unstable during daytime periods.

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The method for calculating $C_{n\ Tatarskii,1971}^2$ that is applied for the surface layer and lower portion of CBL shows a clear negative correlation with height (Figure 5d). Notice that the lower limit of this color bar is much smaller than the others; thus, this method would become highly underestimated above $0.2\ z/z_i$. To deal with that, $C_{n\ Luce,2020}^2$ should be considered within the well-mixed part of CBL (Figure 5e). The decline rate with height is much lower than $C_{n\ Tatarskii,1971}^2$, and it shows the characteristic of CBL where the strongest turbulence activities are mainly within $0.2 \sim 0.8\ z/z_i$ [76]. However, when above $0.8\ z/z_i$, $C_{n\ Luce,2020}^2$ begins to overestimate due to the near-zero variance of potential temperature fluctuations.

Therefore, a combination of these methods is also needed in the vertical detection. In this paper, $C_{n\ Tatarskii,1961}^2$ is used before sunrise, after sunset, and in the region above $0.8\ z/z_i$ of CBL during the daytime. $C_{n\ Tatarskii,1971}^2$ is considered within $0 \sim 0.2\ z/z_i$ and $C_{n\ Luce,2020}^2$ is adopted in the well-mixed part of $0.2 \sim 0.8\ z/z_i$. The combined result is shown in Figure 6d.

By performing comparisons with the TKEDR profile (Figure 4g), it is obvious that there are similar trends between them due to the fact that they are both key parameters used to describe the intensity of turbulence. Nevertheless, the C_n^2 profile reveals more details on the time and space scale because it contains information on both the wind field and meteorological parameters. When temperature stratification is stable during the night-time, the instability of turbulence is mainly driven by wind shear. Moreover, layer structures can be found near the strong wind shear layer (00:00–07:00, 7 September Figure 4f). Correspondingly, during the period around 00:00–03:00, with the increasing intensity of wind shear generated by LLJ, activities in the vertical direction increase (Figure 5a), which causes C_n^2 to rise during the night. In CBL, C_n^2 quickly drops with $z^{4/3}$ in the near-surface layer and then decreases slowly with height in the well-mixed portion.

3.5. Results Analysis

In order to analyze turbulence characteristics in a more comprehensive manner, several key dynamics and thermodynamics parameters are shown in Figure 6. In the profile of the potential temperature (Figure 6a), it increases with height most of the time. In addition, the Brunt–Väisälä frequency squared (Figure 6b) is positive throughout the experiment; however, it is close to zero under CBL during the daytime. By combining these features, we can assume that the atmosphere stratification is stable overall above the CBL and becomes unstable within the CBL.

The gradient Richardson number is also an important and comprehensive turbulence parameter that contains both dynamics and thermodynamics information [56,88,89]. It is a dimensionless number that considers both the effects of buoyancy and wind shear ($R_g = N^2/S^2$), which provides a reference for judging the intensity of atmospheric instability.

If $N^2 < S^2$, turbulence is strengthened due to the domination of wind shear. If $N^2 > S^2$, turbulence is suppressed by the buoyancy term. There is a critical gradient Richardson number (R_c) of 0.25 in order to refer to [90,91]. When $R_g < R_c$, this indicates the small-scale perturbation of turbulence. We point out that R_g is used in stably stratified turbulence, and it becomes much less meaningful when $N^2 < 0$. Therefore, the calculation of R_g in this paper using the "bubble sort" algorithm proposed by Thorpe is meant to re-sort potential temperatures in a monotonically increasing order. Moreover, one should mainly focus on stable stratification conditions. The result of R_g is shown in Figure 6c. Similarly to N^2 , it also has a stably stratified structure outside of CBL and increases after night falls. Significantly, the overall distribution features are quite consistent with C_n^2 .

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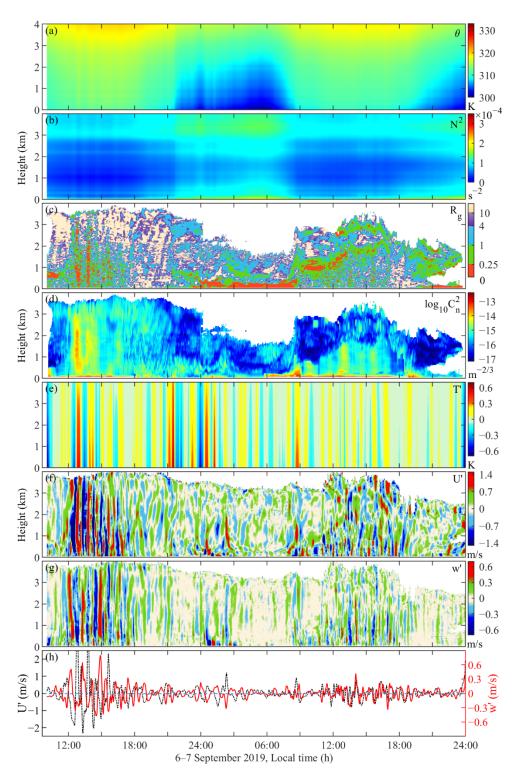


Figure 6. The potential temperature (a), Brunt–Väisälä frequency squared (b), gradient Richardson number (c), $\log_{10}C_n^2$ (d) profiles, perturbations of temperature (e), horizontal wind speed (f), vertical wind speed (g), and averaged wind speed perturbations within 1–2 km (h) derived from CDWL and MWR in the observations on 6–7 September 2019, local time.

Figure 6e–g show the perturbations of temperature, horizontal wind speed, and vertical wind speed, respectively. They are derived from the following procedures. Firstly, the mean background of these parameters is calculated by a moving average with a window of 1 h. Secondly, the original perturbation is the difference between raw data and

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mean background. Thirdly, to reduce high-frequency noises, the original perturbation is smoothed by a moving average of three points. To analyze the wave structures more intuitively, horizontal and vertical wind speeds within the height of 1–2 km are averaged, and then the procedures above are used to obtain the perturbations (Figure 6h).

In the result of C_n^2 (Figure 6d), stratified structures similar to N^2 and R_i can be found outside of CBL, especially on 6 September. In addition, there are several vertical structures in the daytime of C_n^2 on 6 September. By performing comparisons with Figure 6e–h, one can find that they are closely related to the wave structures of T', U', and w'. Unlike gravity waves, these waves are more likely driven by the cloud's ability to block solar radiation, which causes temperature fluctuations. When T' < 0, then w' > 0, indicating that the atmosphere is depositional; on the contrary, the atmosphere is uplifting. These phenomena generate the perturbation of TKEDR directly, which in turn affects the value of C_n^2 .

In Figure 4b, an LLJ with a maximum speed of around 14 m/s formed below 1 km after 21:00 on the sixth, which leads to an increase in wind shear and C_n^2 around it and also the perturbation of temperature. However, what is interesting is that although wind shear is still high after 03:00 and $R_g < R_c$, a large value of N^2 indicates that stratification is quite stable. Therefore, the buoyancy term suppresses the generation of convective activity (vertical wind perturbation is near to zero) and results in a reduction in C_n^2 . In addition, in the area above 1 km from 9:00 to 12:00 on the seventh, the discrepancy between C_n^2 and R_g can also be better understood by the stationary w'.

When estimating R_g and C_n^2 , since the spatial resolution of MWR is lower than CDWL, the original temperature profile is interpolated according to the spatial resolution of CDWL first. The profiles of potential temperature and potential temperature gradient at different times acquired from MWR on 6–7 September are shown in Figure 7a,b,e, and f. The thin lines in Figure 7e,f represent the original profiles of potential temperature gradient calculated by adjacent points. Thick lines represent the potential temperature gradient profiles that are estimated by the moving linear fit in a height range of 200 m. Using these thick lines, the profiles of Brunt–Väisälä frequency squared are shown in Figure 7c,d, which all have a similar characteristic with potential temperature gradient results, as excepted. Then, the gradient Richardson number profiles are depicted in Figure 7g,h.

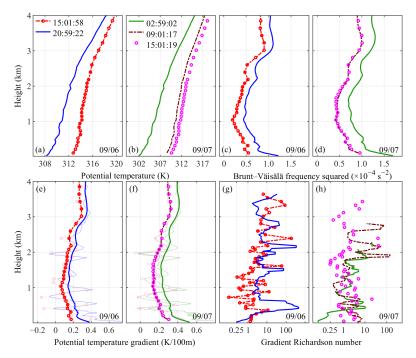


Figure 7. The results of potential temperature (**a**,**b**), potential temperature gradient (**e**,**f**), Brunt–Väisälä frequency squared (**c**,**d**), and gradient Richardson number (**g**,**h**) profiles derived from CDWL, MWR, and the barometric formula at different times on 6–7 September 2019, local time.

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From the profiles of $d\Theta/dz$ and N^2 during the daytime, one can observe that they are normally small and close to zero in the well-mixed part of CBL (Figure 7e,f). Meanwhile, the R_g profiles also have a relatively small value that is less than 1. On the contrary, $d\Theta/dz$, N^2 , and R_g usually have a larger number at night, except for the region where LLJ occurred (Figure 7g,h).

In addition, MWR uses a remote sensing method to obtain the temperature profiles and it has limitations in detecting strong temperature gradient layers [92]. This phenomenon often occurs at the tropopause, the top of the boundary layer, and the inversion layer, particularly at night. In order to analyze these layers more accurately, the spatial resolution of both the MWR and CDWL needs to be highly improved.

Then, the relative error of estimation of TKEDR, combined C_n^2 , and integral scale L_v are calculated vertically in Figure 8. The region with a relative error greater than 50% is marked in light yellow in Figure 8a,b. From the results, it can be observed that when using this combination method to obtain the profiles, a small relative error (Figure 8b, where $RE_{C_n^2}$ is mostly within 30%) can be maintained under CBL. In the meantime, L_v is under 1 km in this area; thus, $R' > L_v$ is satisfied mostly, which results in a low RE_{TKEDR} (Figure 8a). After 18:00, with a decrease in the height of the boundary layer, TKEDR drops rapidly at high altitudes, and L_v becomes larger than 2 km. As a result, the calculated RE_{TKEDR} and $RE_{C_n^2}$ also grow, as shown in the figure. During the period of atmosphere changes from convection to laminar flow (around 18:00 to 21:00), a sudden increase in relative error can be observed, similarly to the horizontal experiment. After the atmosphere stabilized at night, the relative error of TKEDR and C_n^2 began to gradually decrease, but this occurred mainly within the mixing layer.

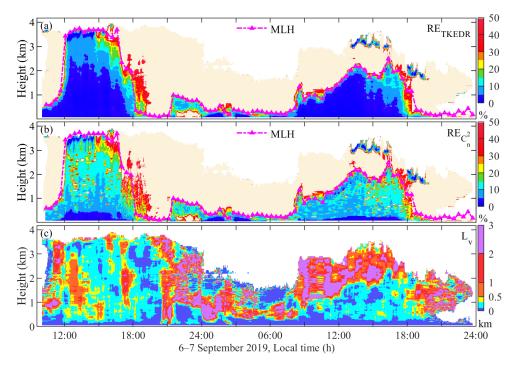


Figure 8. The relative error of the estimation of TKEDR (**a**), combined C_n^2 (**b**), mixing layer height (MLH, (**a**,**b**)), and integral scale L_v (**c**) calculated from CDWL and MWR in the observations from 6 September to 7 September 2019, local time.

To observe different C_n^2 profile characteristics during the day and night, from 15:00 on the sixth to 15:00 on the seventh, five sets of continuous profiles were selected every 6 h for analysis. As shown in Figure 9, each group has six consecutive profiles for a total period of around 12 min. The raw data in original spatial resolution are depicted in black dashed lines, and the blue and red lines represent the results after 100 m and 200 m moving average in the range of 0.03–2.20 km and >2.20 km of the original C_n^2 profiles, respectively.

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In addition, results drawn in the second and third-row represent the profiles of night, which are represented with blue lines, and the remaining rows are the profiles of day, which are depicted as red lines. $RE_{C_n^2}$ is also drawn in every C_n^2 profile with the same color and with a shaded area error bar. The seventh column shows the results of L_v , $l\Delta y$, and R' profiles averaged in 12 min of the corresponding row. Δz profiles are not drawn here because they are smaller than $l\Delta y$ when the height is above 297.7 m.

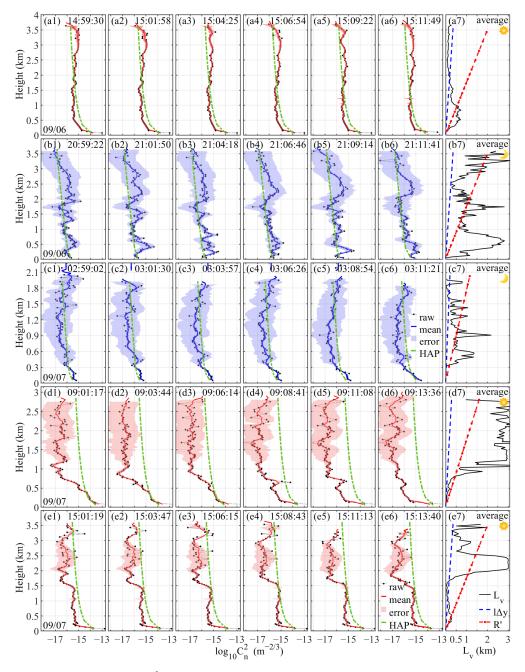


Figure 9. Profiles of $\log_{10}C_n^2$ in raw data that are distance averaged and show a shaded area error bar, calculated from the HAP model and time averaged integral scale L_v (**a7–e7**) during the period of 14:59:30–15:11:49 (**a1–a6**) and 20:59:22–21:11:41 (**b1–b6**) on 6 September and 02:59:02–03:11:21 (**c1–c6**), 09:01:17–09:13:36 (**d1–d6**), and 15:01:19–15:13:40 (**e1–e6**) on 7 September 2019, local time.

As analyzed above, this new combination method holds and has a relatively small uncertainty mostly within CBL. Moreover, strong turbulence activities normally occur in CBL, especially during the daytime. Therefore, to conduct comparisons, the Huf-

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nagel/Andrews/Phillips (HAP) model [27,93] is drawn as green dot-dash lines in Figure 9. The model is a modification of the HV model, which takes into account the power-law relationship with height near the ground, which is more suitable in our experiments considering that $C_{n\ Tatarskii,1971}^2$ is applied within $0 \sim 0.2\ z/z_i$. It can be calculated by the following equation:

$$C_n^2(h) = M \left[0.00594 \left(\frac{w}{27} \right)^2 \left(\frac{h + h_s}{10^5} \right)^{10} e^{-\frac{h + h_s}{1000}} + 2.7 \times 10^{-16} e^{-\frac{h + h_s}{1500}} \right] + C_n^2(h_0) \left(\frac{h_0}{h} \right)^p$$
(37)

where M is a scaling factor that is related to local characteristics (M=1 is applied in this paper), h_s is the height above the sea level, w is the average wind speed in high-altitude (normally 21 m/s), and h_0 and $C_n^2(h_0)$ are the height above the ground of the instrument and the measured C_n^2 , respectively. Power law p typically takes 2/3 at night, and it varies around 4/3 depending on the time during the day (the same as $C_{n\ Tatarskii,1971}^2$).

Firstly, it is not hard to find that the profiles at adjacent moments, especially at night, have a strong correlation and continuity. Secondly, by observing the colored lines, most results at night are one to two orders of magnitude lower than that during the daytime at the same height. In addition, the results of these profiles also show a good agreement with the HAP model, especially within 1.5 km. Similarly to the HAP model, the intensity of C_n^2 decreases distinctly with height, and it drops faster during the day than at night near the ground. Considering that the model is the averaged profile, it is reasonable that the results fluctuate near the profile most of the time. As for the differences in the fourth row, these are mainly due to the boundary layer being uplifted at this moment. In the meantime, the development process of turbulence at different heights can be observed via the high temporal and spatial resolution results of raw data.

In the order of time series, the mean intensity of C_n^2 is the highest around 15:00. After sunset, C_n^2 decreases to the minimum near 03:00. Around 09:00 in the morning, C_n^2 grows from the surface at first but the upper region still remains low. At noon, the profile becomes unstable when C_n^2 reaches the maximum again. All these characteristics reflect the credibility of the results.

By comparing C_n^2 and L_v profiles, one can observe that the $L_v>\max\{\Delta y,\Delta z,l\Delta y\}$ criterion is satisfied under normal conditions, which indicates the credibility of this method in C_n^2 profiling. The $RE_{C_n^2}$ in lower altitudes (especially with CBL) is relatively small due to the high value of CNR, TKEDR, and the low instrumental error of the radial velocity. In these regions, condition $l\Delta y < L_v \ll R'$ is usually satisfied, especially during the daytime. In contrast, in the second and third rows or the high altitude in the fourth and fifth rows, when R' is comparable with or smaller than L_v , the relative error of the estimation of C_n^2 can increase dramatically. C_n^2 can fluctuate between two orders of magnitude above CBL, as shown in the figure.

4. Conclusions and Discussion

To analyze atmospheric turbulence in high resolution, we considered and analyzed three different methods that might be suitable for continuous C_n^2 retrieval. A contrastive experiment was conducted horizontally with LAS to study the characteristics of these methods. By conducting a comparison of a six-day result, it turns out that the methods of C_n^2 Tatarskii,1961, C_n^2 Tatarskii,1971, and C_n^2 Luce,2020 are suitable for stable stratification (outside the CBL), near-surface and lower part of CBL ($0 \sim 0.2 \ z/z_i$), and well-mixed part of CBL ($0.2 \sim 0.8 \ z/z_i$), respectively. A combination of these three methods is then used to work in different circumstances.

Based on the results, we simultaneously obtained the continuous turbulence profiles with high temporal and spatial resolutions. The features and limitations of these methods are also discussed in detail in the vertical experiment. In addition, the dynamic parameters

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such as TKEDR and perturbations of wind were obtained from CDWL. Moreover, MWR can provide the thermodynamic terms such as buoyancy term and the perturbation of temperature. Later, the gradient Richardson number and combined C_n^2 , which contain both dynamics and thermodynamics information, were derived by combining the advantages of CDWL and MWR.

This is significant for studying complex and fast-changing atmospheric environments. Due to the difficulty of C_n^2 profiling with high temporal and spatial resolutions using the existing method, the vertical comparison experiment is hard to achieve. Currently, most researchers adopt the sounding balloon with a radiosonde in the vertical observation; nevertheless, it normally takes a long period of time and its position changes with altitude all the time. Therefore, it is not very suitable for our new method with high temporal and spatial resolutions. More analyses are required in the future for vertical comparison experiments.

We discovered stable stratified structures at night by conducting an analysis of the buoyancy term and gradient Richardson number. The process of demonstrated how turbulence developed from the surface and gradually decreased with height during the day. Moreover, the wave structures were found in the daytime due to the perturbation of temperature and wind speed. Next, by observing continuous typical profiles, the rationality of the results near the surface was verified by comparing them with the HAP turbulence profile model.

Due to the use of CDWL and MWR, there are some limitations of this method that need to be explained. When detecting weak turbulence regions, small-scale turbulence is hard to capture because the volume averaging effect of CDWL can only be corrected to a certain limit. In addition, MWR has difficulties in detecting strong temperature gradient layers. Therefore, the viability of this method in regions such as the tropopause, top of the boundary layer, and inversion layer remains to be further confirmed.

When retrieving vertical profiles, we assumed, most of the time, that the region below CBL satisfies the Kolmogorov "2/3 law" [63]. By performing calculations of the relative error and comparisons between integral scale L_v , $\max\{\Delta y, \Delta z\}$, $l\Delta y$, and R', we analyzed the uncertainty and limitations when using this method at different time periods and altitudes. In the horizontal results, the $L_v>\max\{\Delta y, \Delta z\}$ criterion was proven valid in measuring the credibility of the new method. The compared C_n^2 results showed a great agreement between them most of the time in the six-day experiment, except for the period when the integral scale of turbulence L_v reduces to a value smaller than Δz or $l\Delta y$. In the vertical profiles, C_n^2 can be estimated within the inertial subrange and with a low relative error under CBL. Moreover, L_v grows when TKEDR decreases with height, which leads to a larger $RE_{C_n^2}$ in high altitudes. Therefore, to meet the criterion and to reduce uncertainties as much as possible, the most appropriate scan angle resolution and spatial resolution of CDWL and MRW should be analyzed and adjusted according to the landscape, season, and even time period of the experimental site.

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